

# Statistics Lecture 6



Feb 19-8:47 AM

**Addition Rule** (S&T 11)

Keyword OR

Single Action Event

$$P(A \text{ or } B) = P(A) + P(B) - P(\text{A and B})$$

Both

Ex:  $P(A) = .2$ ,  $P(B) = .7$ ,  $P(A \text{ and } B) = .1$

1)  $P(\overline{A}) = 1 - P(A) = 1 - .2 = .8 \Rightarrow P(\overline{B}) = 1 - P(B) = 1 - .7 = .3$

Complement Rule

3)  $P(\overline{A \text{ and } B}) = 1 - P(A \text{ and } B) = 1 - .1 = .9$

4)  $P(A \text{ or } B) = P(A) + P(B) - P(A \text{ and } B)$   
 Addition Rule  $= .2 + .7 - .1 = .8$

Venn Diagram

$P(A \text{ only}) = .2 - .1 = .1$

$P(B \text{ only}) = .7 - .1 = .6$

Total = 1

$P(\overline{A \text{ or } B}) = 1 - P(A \text{ or } B) = 1 - .8 = .2$

Complement Rule

Oct 4-11:35 AM

$P(HB) = .45$       1)  $P(\overline{HB}) = 1 - .45 = \boxed{.55}$   
 $P(FF) = .35$       Complement Rule  
                                  2)  $P(\overline{FF}) = 1 - .35 = \boxed{.65}$

$P(\text{HB and FF}) = .2$   
                                  both (overlap)

$P(\text{HB or FF}) = P(HB) + P(FF) - P(\text{HB and FF})$   
                                  Addition Rule       $= .45 + .35 - .2 = \boxed{.6}$

$P(\overline{\text{HB and FF}}) = 1 - P(\text{HB and FF}) = 1 - .2 = \boxed{.8}$   
                                  Complement Rule

$P(\overline{\text{HB or FF}}) = 1 - P(\text{HB or FF}) = 1 - .6 = \boxed{.4}$

Construct Venn Diagram

$P(\text{HB only}) = .45 - .2 = .25$   
 $P(\text{FF only}) = .35 - .2 = .15$

$P(\text{HB or FF but not both}) = .25 + .15 = \boxed{.4}$

Oct 4-11:46 AM

**Mutually Exclusive Events**  
**Disjointed Events**

They don't happen together

No overlap

If A and B are **M.E.E.**  $\iff P(A \text{ and } B) = 0$

Oct 4-11:57 AM

$P(A) = .3$  ,  $P(B) = .5$  , A and B are M.E.E.

1)  $P(\bar{A}) = 1 - P(A) = \boxed{.7}$

2)  $P(\bar{B}) = 1 - P(B) = \boxed{.5}$

3)  $P(A \text{ and } B) = \boxed{0}$

4)  $P(\overline{A \text{ and } B}) = 1 - P(A \text{ and } B) = 1 - 0 = \boxed{1}$

5)  $P(A \text{ or } B) = P(A) + P(B) - P(A \text{ and } B)$   
 $= .3 + .5 - 0 = \boxed{.8}$

6)  $P(\overline{A \text{ or } B}) = 1 - P(A \text{ or } B) = 1 - .8 = \boxed{.2}$

Construct Venn Diagram

Total = 1

Oct 4-12:00 PM

De Morgan's Law:

$P(\bar{A} \text{ and } \bar{B}) = P(\overline{A \text{ or } B})$   
 $P(\bar{A} \text{ or } \bar{B}) = P(\overline{A \text{ and } B})$

$P(A) = .4$      $P(B) = .8$      $P(A \text{ and } B) = .3$

1)  $P(\bar{A}) = 1 - .4 = \boxed{.6}$     2)  $P(\bar{B}) = 1 - .8 = \boxed{.2}$

3)  $P(A \text{ or } B) = P(A) + P(B) - P(A \text{ and } B)$   
 $= .4 + .8 - .3 = \boxed{.9}$

4) Construct Venn Diagram    Total = 1

$P(A \text{ only}) = .4 - .3 = .1$

$P(B \text{ only}) = .8 - .3 = .5$

$P(A \text{ only OR } B \text{ only}) = .1 + .5 = \boxed{.6}$

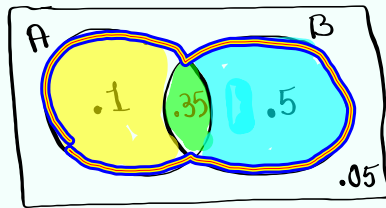
$P(\bar{A} \text{ and } \bar{B}) = P(\overline{A \text{ or } B}) = 1 - P(A \text{ or } B) = 1 - .9 = \boxed{.1}$

De Morgan's Law

$P(\bar{A} \text{ or } \bar{B}) = P(\overline{A \text{ and } B}) = 1 - P(A \text{ and } B) = 1 - .3 = \boxed{.7}$

Oct 4-12:10 PM

Complete the Venn Diagram below:



1)  $P(A \text{ and } B) = .35$

2)  $P(\overline{A \text{ and } B}) = .65$

3)  $P(A \text{ only}) = .1$

4)  $P(A) = .45$

5)  $P(B \text{ only}) = .5$

6)  $P(B) = .85$

7)  $P(A \text{ or } B) = .95$

8)  $P(\overline{A \text{ or } B}) = .05$

9)  $P(\overline{A} \text{ and } \overline{B}) = P(\overline{A \text{ or } B}) = .05$

De Morgan's Law

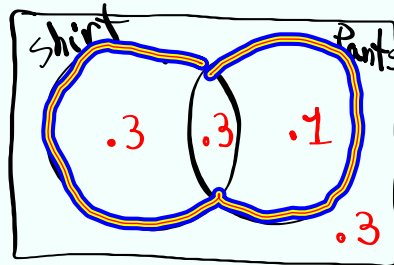
10)  $P(\overline{A} \text{ or } \overline{B}) = P(\overline{A \text{ and } B}) = .65$

Oct 4-12:21 PM

$P(\text{shirt}) = .6$  ✓

$P(\text{pants}) = .4$  ✓

$P(\text{shirt and pants}) = .3$



Total = 1

1) Construct Venn Diagram

2)  $P(\text{shirt or pants}) = P(\text{shirt}) + P(\text{pants}) - P(\text{both})$

SE 11 ✓

Addition Rule

$= .6 + .4 - .3$   
 $= .7$

Oct 4-12:31 PM